

A-822

M.Sc. II Semester ATKT Examination 2020

Subject : Mathematics

Paper : I – Complex Analysis

Max.Marks : 15

Note: Attempt any five questions.

1. State and prove Schwarz Lemma.
2. Show that the function e^z has an isolated essential singularity at $z=\infty$.
3. Apply the calculus of Residue to prove that
$$\int_0^{\infty} \frac{dx}{1+x^2} = \frac{\pi}{2}$$
4. If $f(z) = u + iv$ is analytic function and $u - v = e^x(\cos y - \sin y)$. Find $f(z)$ in term of z .
5. State and prove Morera's theorem.
6. State and prove Maximum Modulus principle.
7. State and prove Hurwitz theorem.
8. State and prove Cauchy's Residue theorem.
